

**Melt modeling:
Temperatur-index models vs.
Energy balance models**

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(Slides: modified from R. Hock)

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How to model melt ?

- 1. **Physically based energy-balance models:** each of the relevant energy fluxes at the glacier surface is computed from physically based calculations using direct measurements of the necessary meteorological variables
- 2. **Temperature-index or degree-day models:** melt is calculated from an empirical formula as a function of air temperature alone

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Melt Modelling

Temperature index | **Energy balance**

Data requirements Model sophistication

Input data:
Air temp | Air temp, humidity, wind speed, radiation, ****

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Mass balance models

0-Dim | **elevation bands** | **fully distributed**

Spatial discretization

Model type

1 Temp-index regression | 2 Temp-index or simplified energy balance | 3 Energy balance

Increasing model sophistication

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Temperature-index melt models

- Assume a relationship between air temperature and melt: $M=f(T)$, $M=f(T^*)$

Relationship melt - air temperature

Qamanbrisp sermie
June, July & August, 1980-86

Qamanbrisp sermie
1980-1986

Relationship melt - air temperature

Data by R. Braithwaite

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Temperature-index melt models

- Assume a relationship between air temperature and melt: $M=f(T)$, $M=f(T^*)$

Relationship melt - degree-day sum

Positive degree-day sum
 $PDD = \sum T^+$

Ice ablation mm water

Degree-days deg d

Monthly equivalent

Legend: GAM, NBG, IMAU, AWI, EGIS

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Physical basis of temp-index models

Air temperature directly affects several components of the surface energy balance

Longwave incoming rad $L_{\downarrow} = \epsilon \sigma T^4$

Sensible heat flux $f(T)$

Latent heat flux $f(e(T))$

$$Q_M = G(1-\alpha) + L_{\downarrow} - L_{\uparrow} + Q_H + Q_L$$

- Longwave incoming radiation (L_{\downarrow}) is the largest contribution to melt (~70%) (Ohmura, 2001: Physical basis of temperature-index models)
- L_{\downarrow} has low variability compared to other fluxes

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Spatial variability of degree-day factors

Calculation of degree-day factors for various points on the Greenland ice sheet with an atmospheric and snow model (thesis Filip Lefebre)

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Degree-day factors [mm/day/K]

Spatial and diurnal variation
Derived from energy balance modeling

$$M = DDF_{ice/snow} \cdot T^+$$

Heck, 1999, J. Glaciol.

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Modified temperature-index model

Including potential direct solar radiation

Classical degree-day factor $M = DDF_{ice/snow} \cdot T^+$

Including pot. direct radiation $M = (MF + a_{ice/snow} \cdot DIR) \cdot T^+$

Model introduces

- a spatial variation in melt factors
- a diurnal variation in melt factors

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Modified temperature-index model

Simulated cumulative

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Distributed temp-index model

$$M = TF \cdot T + AF \cdot (1-\alpha) \cdot I \quad T > T_T$$

Temperature

Albedo

Incoming shortwave radiation

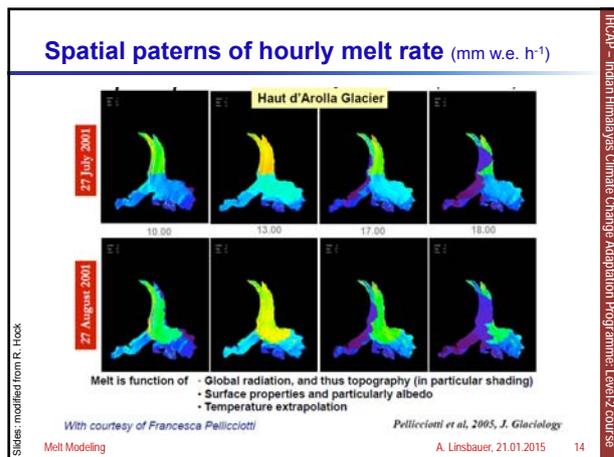
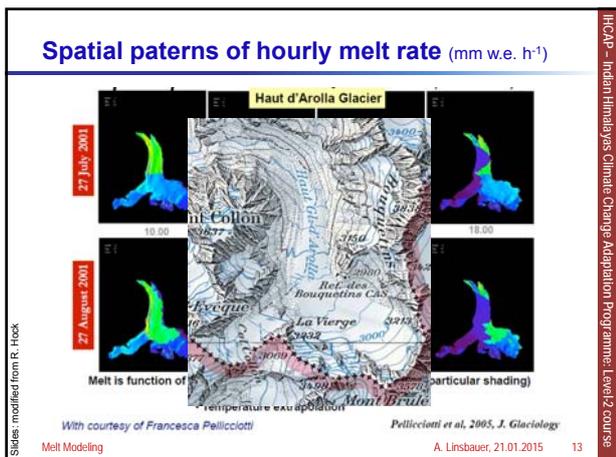
Computed as function of accumulated maximum daily temperature since snowfall
Brock et al. (2000)

Computed as function of daily temperature range

Model only requires air temperature
Global radiation and albedo parameterized

Pellicciotti et al, 2005, J. Glaciology

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Simplified energy balance model

Oerlemans (2001)

$$M = a * R + \text{melt factor} * T$$

$$M = (1-\alpha)G + c_0 + c_1T$$

Shortwave radiation balance Longwave balance and turbulent fluxes

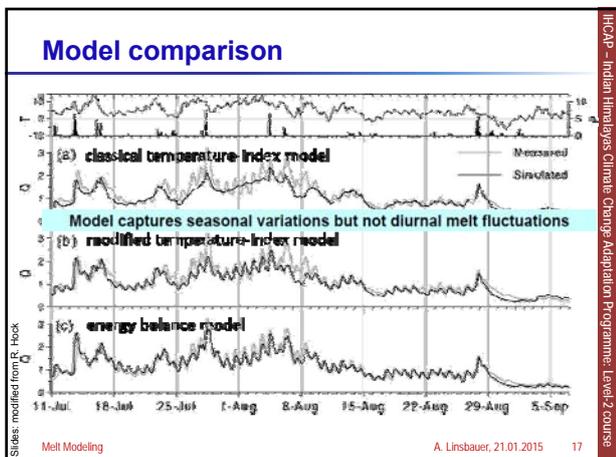
→ Gradual transition from degree-day models to energy balance-type expressions by increasing the number of climate input variables

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Temperature-index versus energy balance

| | Temperature index | Energy balance |
|---------------------|---|---|
| Advantages | <ul style="list-style-type: none"> Wide availability of Temp-data Easy interpolation and forecasting Good model performance Computational simplicity | <ul style="list-style-type: none"> Physical based – describe physical processes more adequately Projections more reliable |
| Shortcomings | <ul style="list-style-type: none"> Empirical, not physically based DDF vary, works on 'average conditions' Does not work in tropics Model parameter stability under different climate conditions? | <ul style="list-style-type: none"> Large data requirements (often not available) |

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Summary

- Both temp-index and energy balance models are useful tools, choice depends on data availability
- Awareness of limitations
- Need for more approaches of intermediate complexity and moderate data input
- Both temp-index and energy balance models need calibration (parameter tuning)

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